

Government College of Engineering and Research, Avasari(Khurd)

Department: Mechanical Engineering

Learning Resource Material (LRM)

Name of the course: Mechanical System Design **Course Code:** 402048

Name of the faculty: J. M. Arackal **Class:** BE(Mech)

SYLLABUS(Unit 3)

Unit 3: Design of Belt conveyer system for material handling (8 Hours)

System concept, basic principles, objectives of material handling system, unit load and containerization.

Belt conveyors, Flat belt and troughed belt conveyors, capacity of conveyor, rubber covered and fabric

ply belts, belt tensions, conveyor pulleys, belt idlers, tension take-up systems, power requirement of horizontal belt conveyors for frictional resistance of idler and pulleys.

Lecture Plan format:**Name of the course:** Mechanical System Design **Course Code** 402048

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Unit No	Lecture No.	Topics to be covered	Text/Reference Book/ Web Reference
		UNIT 3	
3	1	System concept, basic principles, objectives of material handling system	1,2
3	2	Unit load and containerization. Belt conveyors, Flat belt and troughed belt conveyors	1,2
3	3	Capacity of conveyor, rubber covered and fabric ply belts	1,2
3	4	Belt tensions, conveyor pulleys, belt idlers, tension take-up systems	1,2
3	5	Power requirement of horizontal belt conveyors for frictional resistance of idler and pulleys.	1,2
3	6	Problems On Material Flow Capacity etc.	1,2
3	7	Problems On Material Flow Capacity etc.	1,2
3	8	Slack side to Tight side force calculation and Power Requirements	1,2

List of Text Books /Reference Books/ Web Reference*1-Bhandari V.B. —Design of Machine Elements*, Tata McGraw Hill Pub. Co. Ltd.*2-R.K. Jain- Machine Design, Khanna Publishers**3-Johnson R.C., —Mechanical Design Synthesis with Optimization Applications*, Von Nostrand Reynold Pub

Design of Material Handling System.

Material Handling

- Picking up Load
- Transporting
- Placing the load.

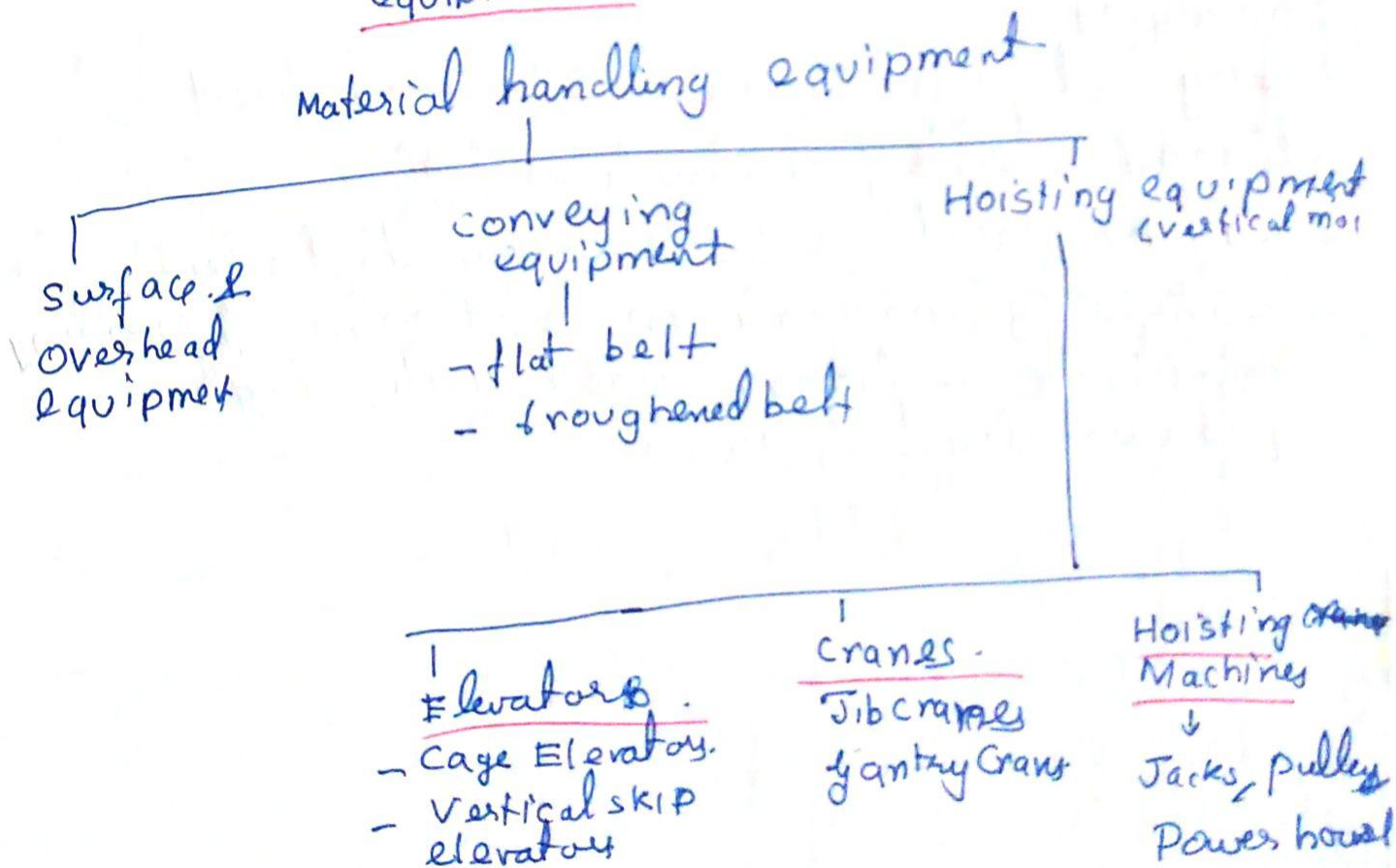
Types of Load

- Bulk Load - Lumps of material, coal, sand, etc.
- Unit Load - Rigid & Single. - machine boxes, containers

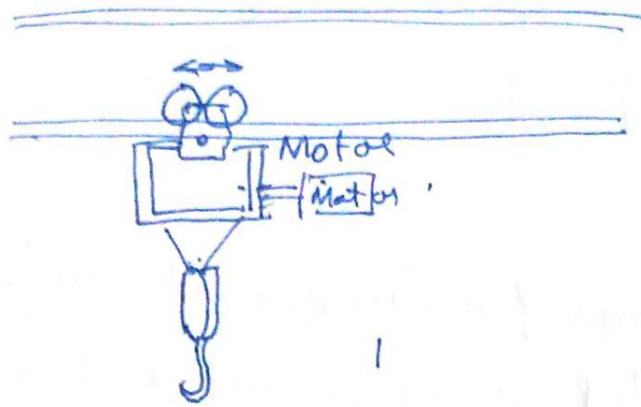
Containerization

Special type of unit load.
converting bulk load to unit load.
size containers based on load to be handled.
space available.

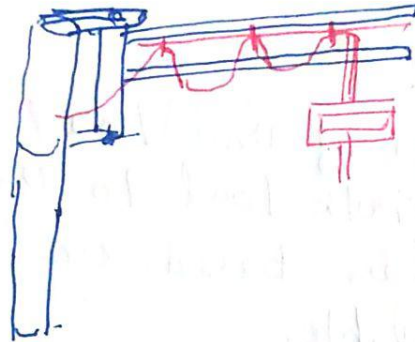
Classification of Material Handling Equipment



Hoisting - power operated



Tab Crane.



Conveying equipments Horizontal / Inclined directions

conveyors

- Carry loads in horizontal & inclined direction.
- Transfer rate of materials is high.
- Can be placed on floor, or at higher level.
- Can carry materials in extreme operating conditions - furnace, paint units, high pressure cleaning units

Types of Materials Handled by Conveyors:

2

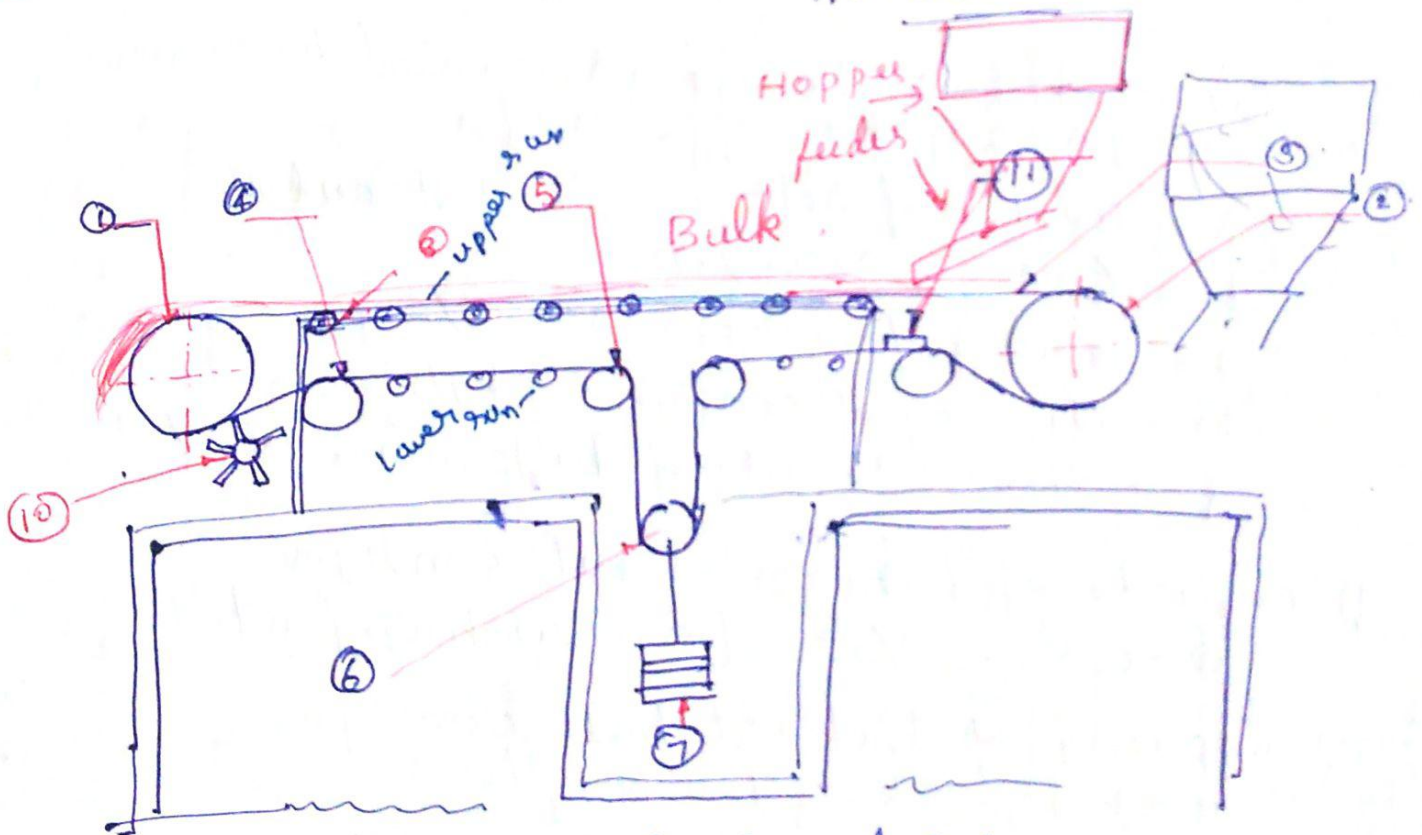
- Bulk materials
- Hazardous materials
- Loose materials
- Packages

Types of Conveyors

- Flat belt
- Troughed Belt conveyors
- Blanket Belt conveyors
- Woven wire conveyors
- chain conveyors
- Apron conveyors
- screw conveyors

- 1- Head pulley
- 2- Tail pulley
- 3- Conveyor belt
- 4- Snub pulley
- 5- Bend pulley
- 6- Takeup pulley
- 7- Counterweight
- 8- Idlers/Rollers
- 9- Return idlers
- 10- Belt cleaners (Scrapers)
- 11- Internal belt cleaner

Flat belt conveyor



Layout of flat belt conveyor

Methods of feeding or loading to Flat belt conveyors

- 1) By hooper.
- 2) By preceding conveyor
- 3) By process equipment
- 4) By travelling machine. (travelling hook)

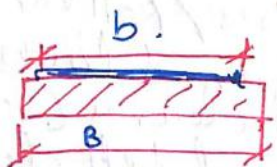


Troughed belt conveyors

width of flat belt limits the volume carrying capacity

Trough shape given by idler pulley.
nylon / Polymer / polyester belts are used.

Capacity of Belt conveyors (Q)



Belt.



Three Idler Troughed Belt

B = width of the belt.
b = width of material stored on belt or effective belt width

Rate at which material is carried by conveyor is known as capacity of conveyor.

B = width of belt, v = belt speed m/s

$b = (0.9B - 0.05) m$.

Q = Capacity of conveyor in m^3/s .

M = Capacity of conveyor in kg/s.

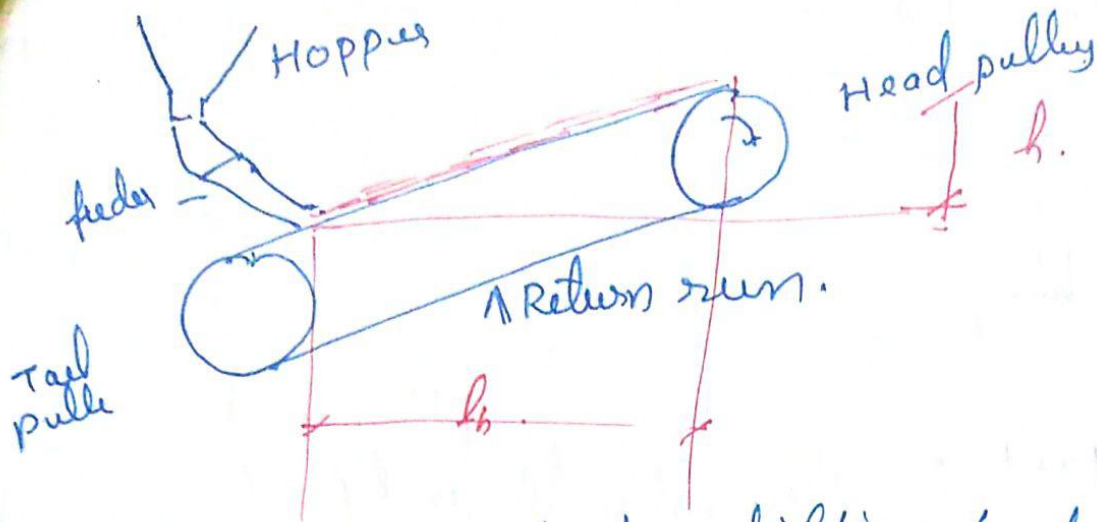
ρ = mass density of bulk material kg/m^3

1) Capacity of horizontal belt conveyor
 $Q = C b^2 v$ (m^3/s). [C = surcharge factor]

2) Capacity of inclined belt conveyor
 $Q = k b^2 v$ k = flowability factor

⇒ standard Belt widths are there,

Power Requirement of Belt Pulley Conveyor.



- Power required for lifting load.

$$\begin{aligned} \text{Power} &= \frac{wD}{s} \\ &= \frac{\text{mass lifted} \times g \times h}{\text{time(s)}} \\ &= \frac{M \times g \times h}{\text{sec}} \quad [M = \text{kg/s}] \end{aligned}$$

we have $\rho \times Q = M$
 $(\frac{\text{kg}}{\text{m}^3} \times \frac{\text{m}^3}{\text{s}})$

$$\text{Power} = \frac{\rho Q g h}{1000} \text{ kw} \quad (P_e)$$

- Power required for overcoming frictional resistance.

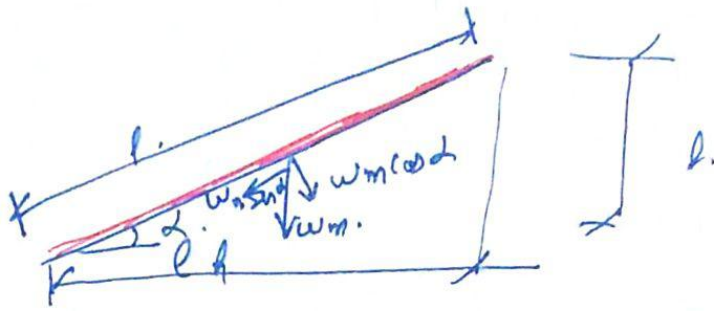
$$P_f = \frac{C_o l \rho g Z}{1000} \text{ kw} \quad [l = \text{length of the belt}]$$

$$P = P_e + P_f$$

$C_o =$ specific friction factor

Analysis of power requirement of Belt conveyor

1) Load resistance due to lifting of Material



l = length of load carrying run of belt.
 h = height through which material is lifted.

l_2 = length of return run of belt.

v = belt speed (m/s).

m_m = material carried by conveyor per unit length of belt (kg/m).

α = angle of inclination of belt.

Total load carrying run of the belt is

$$W_m = m_m \times l \times g$$

This is resolved as

$$W_m \cos \alpha = m_m l g \cos \alpha \quad (\text{acts as normal reaction on idlers})$$

$$W_m \sin \alpha = m_m l g \sin \alpha \quad (\text{direction opposite to belt motion \& its termed as load resistance})$$

$$= m_m l g \sin \alpha$$

$$F_{m.l} = m_m g h \quad (\text{component along the belt})$$

A horizontal flat belt conveyor is used for transporting the bulk material having mass density of 2000 kg/m^3 . The surcharge factor 'c' for the flat belt is 0.075, while the belt width is 800 mm. If the belt speed is 1.75 m/s determine the capacity of conveyor. (Q & M).

m) we have $Q = cb^2v$. (m^3/s)

where $b = (0.9B - 0.05) \text{ m}$.

$c = 0.075$

$Q = 0.075 (0.9 \times 8 - 0.05)^2 \times 1.75$

$Q = 212.1 \text{ m}^3/\text{h}$

$m = \rho Q \text{ kg/h}$

$= 2000 \times 212.1$

$= 424.2 \times 10^3 \text{ kg/h} = 424.2 \text{ ton/h}$

Q) A three idler, troughed belt, horizontal conveyor is to be used for transporting 350 ton/h of mineral ore having weight density of 16700 N/m^3 . The surcharge factor 'c' for the three idler troughed belt is 0.1. If the belt speed is 120 m/min. Select the standard belt width for the conveyor belt.

Available standard belt widths are,

400, 450, 500, 600, 650, 750, 800, 900

1000, 1200, 1400, 1600, 1800, 2000 mm

$$Q = C b^2 v.$$

$$b = (0.9B - 0.05)$$

$$v = \frac{120}{60} = 2 \text{ m/s.}$$

we have. $M = \rho Q.$

$$M = \frac{350 \times 10^3}{3600} = 97.2 \text{ kg/s.}$$

$$\therefore 97.2 = \rho Q$$

$$\rho = \frac{16700 \text{ N/m}^3}{9.81} = 1702.34 \text{ kg/m}^3$$

$$\therefore Q = \frac{97.2}{\rho} = \frac{97.2}{1702.34}$$

$$\Rightarrow Q = C b^2 v.$$

$$b = \sqrt{\frac{Q}{Cv}} = \sqrt{\frac{97.2}{1702.34 \times 0.1 \times 2}}$$

$$b = 0.534.$$

$$\Rightarrow (0.9B - 0.05) = 0.534 \text{ m}$$

$$\therefore \boxed{B = 650 \text{ mm}}$$

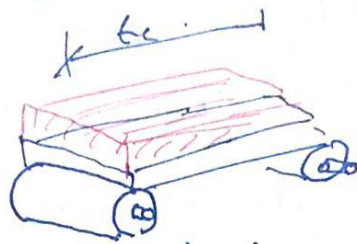
$$\frac{\text{kg}}{\text{m}^3}$$

$$m = \rho Q$$

$$M = \frac{\text{kg}}{\text{m}^3} \times \frac{\text{m}^3}{\text{s}}$$

Analysis of

2) frictional resistance . Due to idlers



m_m = mass/unit length of mass of material carried by conveyer / unit belt length

m_b = mass of belt / unit length.

m_i = mass of each idler.

t_c = pitch of carrying run idlers

t_r = pitch of return run idlers

Z_c = no of carrying run idlers

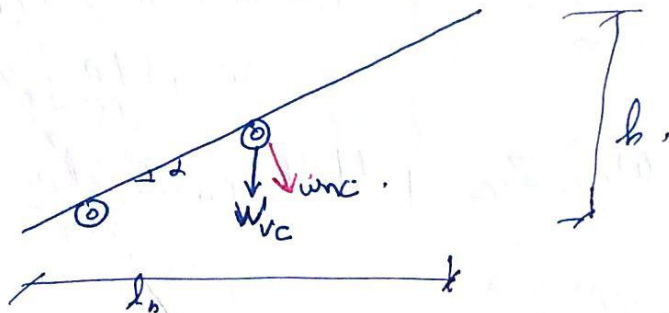
Z_r = no of return run idlers

d_i = dia of idler

d_p = dia of idler pin.

μ_{ir} = coefficient of friction between idler & belt.

μ_{ip} = coefficient of friction between idler & idler pin



vertical load on each idler is

$$W_{vc} = (m_b + m_m) \cdot g \cdot t_c$$

$$w_{nc} = (m_b + m_m) \cdot g \cdot t_c \cdot \cos \alpha$$

∴ frictional force.

$$\mu_s W_{nc} = \mu_s (m_m + m_b) g t_c \cos \alpha.$$

Total frictional force

$$\mu_s W_{nc} Z_c = \mu_s (m_b + m_m) (g t_c \cos \alpha) Z_c.$$

$$= \mu_s (m_m + m_b) g l \cos \alpha \quad [\because t_c Z_c = l]$$

$$\mu_s W_{nc} Z_c = \mu_s (m_m + m_b) g l \cos \alpha.$$

Load on the pin of idler. (each pin)

$$W_{pin} = W_{rc} + m_i g.$$

$$= (m_m + m_b) g t_c + m_i g.$$

frictional resistance per pin.

$$\mu W_{pin} = \mu [(m_m + m_b) g t_c + m_i g].$$

∴ Total frictional resistance

$$\mu_p W_{pin} \times Z_c = \mu [(m_m + m_b) g t_c + m_i g] Z_c.$$

∴ Total frictional resistance.

$$= \mu W$$

equivalent friction due to pin & rollers.

is

$$\mu_p W_{pin} \times Z_c \frac{dP}{ds} = \mu [(m_m + m_b) g t_c \frac{dP}{ds} + m_i g \frac{dP}{ds}] Z_c.$$

$$\therefore \text{Total} = \mu_s W_{nc} Z_c + \mu_p W_{pin} Z_c \frac{dP}{ds}.$$

frictional
resistance.

due to carrying
sum of rollers.

$$F_{CR1} = f_c (m_m + m_b + \frac{m_i Z_c}{l}) g l.$$

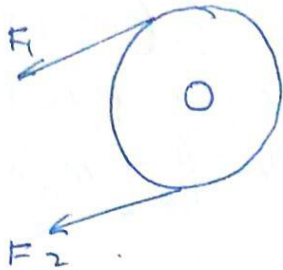
f_c = friction
factor

Frictional resistance due to return idlers.

$$F_{ri} = f_c \left[m_b + \frac{m_i z_s}{l} \right] g l_s$$

Frictional Resistance due at Pulley.

Let



\$m_p\$ = mass of pulley
 \$d_B\$ = dia of bearings
 \$D_p\$ = Dia of pulley.

$$F_p = \mu \left[(F_1 + F_2) + m_p g \right] \frac{d_B}{D_p}$$

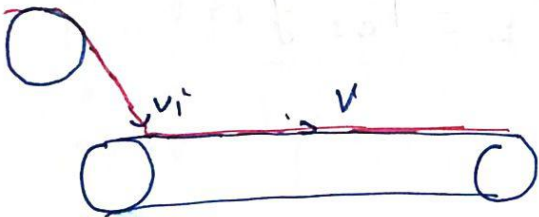
(Equivalent)

\$\therefore\$ Empirical relation

$$F_p = \epsilon F_1$$

where \$\epsilon\$ = angle of lap (or snub) factor for pulley.

4) Resistance at Loading station.



$$F_L = M (v - v_1)$$

\$\therefore\$ \$M\$ = mass of material (kg/s)

5) Frictional resistance at Unloading station

$$F_u = (3.1 \text{ to } 3.6) m_u g B$$

6) Frictional resistance at Cleaning station.

$$F_{CL} = k_{CL} g B$$

Resisting force.

Expression.

1. Load due to lifting of material

$$F_m = m_m g h$$

2. Frictional resistance due to idlers.

$$F_{ci} = f_c \left(m_m + m_b + \frac{m_i z_c}{L} \right) g L$$

(Carry run)

$$F_{cs} = f_c \left(m_b + \frac{m_i z_s}{L} \right) g L_s$$

3. Frictional resistance due to pulley

$$F_p = \mu_p W \frac{d_b}{D_p}$$

or

$$F_p = \epsilon F_{p1}$$

4. Resistance at Loading station

$$F_L = M (V - V_i)$$

5. Frictional Resistance at Unloading (F_u) (Removal by plough)

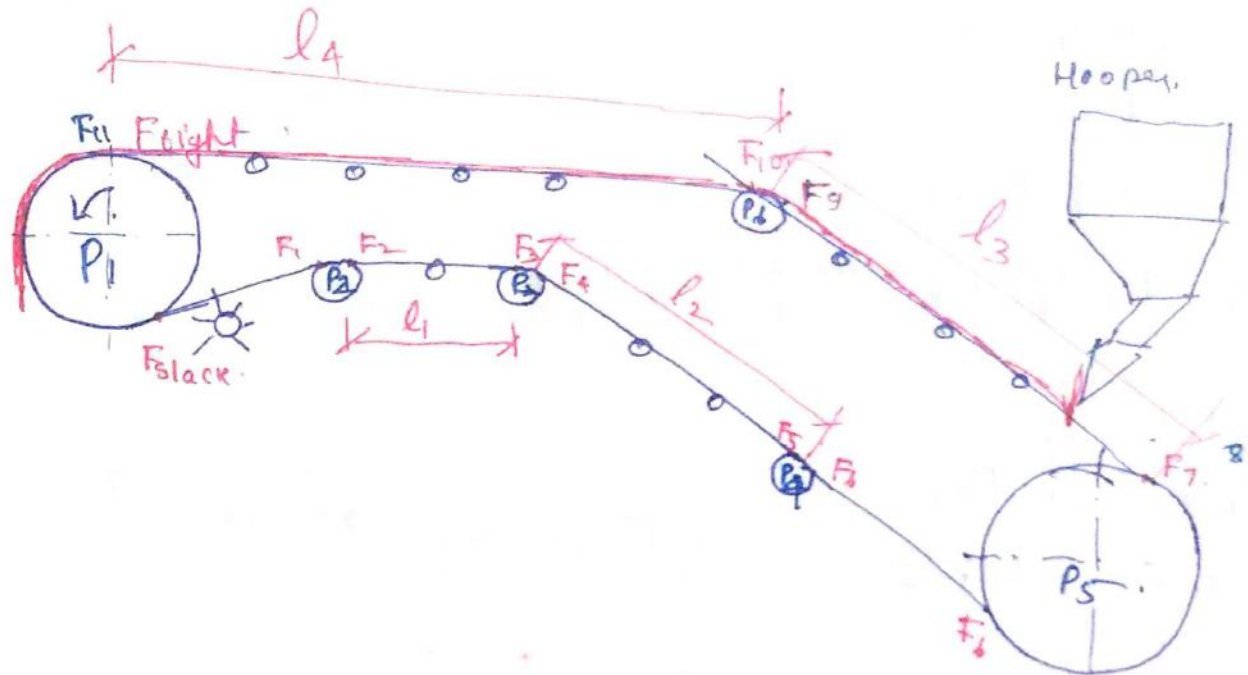
$$F_u = (3.1 \text{ to } 3.6) m_m g B$$

6. Frictional Resistance at cleaning station (F_{cl})

$$F_{cl} = k_{cl} g B$$

Belt tensions
Various points

antism idlers.



The belt tension at every succeeding point is equal to the belt tension at the preceding point plus the resulting force within the section between the two points.

Let F_{slack} = Effective tension on slack side.

F_{tight} = Effective tension in tight side. [start where belt leaves & end when it comes back to drive]

At initial point.

$$F_i = F_{slack}$$

At point 1 $F_1 = F_{slack} + F_{c1}$
 $= F_{slack} + K_{c1} g B.$

At point 2 $F_2 = F_1 + F_{p2}$
 $= F_1 + E_{p2} F_1.$

At point 3 $F_3 = F_2 + F_{\pi\pi}$
 $F_3 = F_2 + f_c \left[\frac{m_b + \frac{m_i z_{\pi}}{l_1}}{l_1} \right] g l_1$

At point 4

$$F_4 = F_3 + F_{p3}$$

$$= F_3 + \epsilon_{p3} F_3$$

At point 5

$$F_5 = F_4 + F_{r24}$$

$$F_5 = F_4 + f_c \left(m_b + \frac{m_i z_{r2}}{l_2} \right) g l_2$$

At point 6

$$F_6 = F_5 + F_{p5}$$

$$= F_5 + \epsilon_{p4} F_5$$

[$\epsilon_p =$ snub for respective pulley]

At point 7

$$F_7 = F_6 + F_{p6}$$

$$= F_6 + \epsilon_{p5} F_6$$

At point 8

$$F_8 = F_7 + F_L$$

$$F_8 = F_7 + M (v - v_i)$$

At point 9

$$F_9 = F_8 + F_{c3} + F_m$$

$$F_9 = F_8 + f_c \left[m_m + m_b + \frac{m_i z_{c3}}{l_3} \right] g l_3 + m_m g h$$

At point 10

$$F_{10} = F_9 + \epsilon_{p6} F_9$$

At point 11

$$F_{11} = F_{10} + F_{c4} + F_u$$

At final point

$$F_{\text{right}} = F_{11} + F_{p1}$$

$$= F_{11} + \epsilon_{p1} F_{11}$$

Again we have

3

$$\frac{F_{\text{tight}}}{F_{\text{slack}}} = e^{\mu \alpha}$$

$$P_0 = \text{Power required to drive pulley} = \frac{(F_{\text{tight}} - F_{\text{slack}}) v}{1000} \text{ kW}$$

$$P_{\text{input power}} = \frac{P_0}{\eta}$$

Selection of number of plies for conveyor belts

Let F_{bs} = breaking strength of conveyor belt

$$F_{bs} = (FOS) F_{tmax} \quad [F_{tmax} = \text{Max tension in the belt}]$$

$$F_{bs} = S_u \cdot B \cdot Z_p$$

where S_u = UTS per unit width of ply.

Z_p = No of plies

Min. Dia of Pulley

$$D_{\text{min}} = k_1 k_2 Z_p$$

when k_1 = Material factor for plies

k_2 = Belt tension & arc of contact factor

a) A belt conveyor is to be designed to carry the bulk material at the rate of 300×10^3 kg/hr with following details.

Bulk density of the material = 800 kg/m^3 .

Angle of repose of the bulk material = 15°

Belt speed = 10 km/hr .

Material factor for plies, $k_1 = 2$

Belt tension & arc of

contact factor, $k_2 = 6.3$

At point 4

No of plies for the belt = 4.

Surcharge factor $15^\circ = 0.075$.

Determine:

i) Suitable width for the belt

ii) Dia & length of Drive pulley.

Ans) $Q = cb^2v$.

$$b = (0.9B - 0.05)$$

$$M = \rho Q$$

$$\therefore \rho = \frac{M}{Q}$$

$$M = Cb^2v\rho$$

$$M = C(0.9B - 0.05)^2 v \rho \quad \text{--- (1)}$$

$$800 = 0.075(0.9B - 0.05)$$

$$M = \frac{300 \times 10^3}{3600}$$

$$\text{kg/s} = 83.33 \text{ kg/s}$$

$$v = 10 \text{ km/hr} = \frac{10 \times 10^3}{3600} = 2.77 \text{ m/s}$$

$M = \dots$ Put all in (1).

$$83.33 = 0.075(0.9B - 0.05)^2 \times 2.77 \times 800$$

$$(0.9B - 0.05)^2 = \frac{40123}{0.5}$$

$$0.9B - 0.05 = 0.708$$

$$B = 842.3 \text{ mm}$$

$$\boxed{B \approx 850 \text{ mm}}$$

ii) Dia of pulley = $k_1 k_2 z_p$

$$= 2 \times 63 \times 4 = 504$$

$$\approx 510 \text{ mm}$$

length of pulley = $B + 250$

$$= 850 + 150$$

$$= 1000 \text{ mm}$$

$$= 1000 \text{ mm}$$

we have.

$$V = \frac{\pi D N}{60}$$

$$\frac{90}{60} = \frac{\pi \times 480 \times N}{60}$$

$$N = 60 \text{ rpm}$$

$$\therefore \text{Reduction ratio} = \frac{1440}{60}$$

$$G = 2.4$$



- Q) A triple ply belt conveyor is required to transport 1.5 ton of iron ore per hour through a distance of 800 m on ground & height of 300 m. The permissible belt speed is 75 m/min. If the mass density of iron ore is 2.5 ton/cubic metre. determine.
- belt width.
 - The dia of the drive pulley.
 - The reduction ratio of gear reducer, if electric motor speed is 1440 rpm.
- use following data:

Belt Inclination (α).	10°-15°	16-20	21-25	26-30	31-35
flowability factor k .	2.65×10^{-4}	2.5×10^{-4}	2.35×10^{-4}	2.20×10^{-4}	2.05×10^{-4}

Standard belt width: 400, 450, 500, 600, 650, 750, 800, 900, 1000, 1200, 1400, 1600, 1800, 2000 mm.

Material factor for plies for carbon belt: $k_1 = 2$

Belt tension & arc of contact factor: $k_2 = 80$.

$$M = 2 \text{ tons/hr.} = 2 \times 10^3 \text{ kg/hr}$$

$$\frac{\quad}{1000} \Big| 300$$

$$V = 90 \text{ m/min.}$$

$$\rho = 2.5 \times 10^3 \text{ kg/m}^3$$

we have .

$$Q = C b v^2 = k b v^2 \text{ (Inclined hel)}$$

$$M = \rho Q$$

$$M = \rho k b v^2$$

for selecting k we need to find inclination α .

$$\frac{\quad}{1000} \Big| 300$$

$$\tan \alpha = \frac{300}{1000}$$

$$\alpha = 16.7^\circ$$

\therefore from table

$$k = 2.5 \times 10^{-4}$$

$$b = (0.9B - 0.05)$$

$$M = \rho k b v^2$$

$$M = \frac{2 \times 10^3}{3600} = 0.55 \text{ kg/s.}$$

$$k = 2.5 \times 10^{-4}$$

$$\rho = 2.5 \times 10^3 \text{ kg/m}^3$$

$$V = \frac{90}{60} = 1.5 \text{ m/min}$$

$$0.55 = 2.5 \times 10^3 \times 2.5 \times 10^{-4} \times 1.5^2 (0.9B - 0.05)^2$$

$$\therefore 0.9B - 0.05 = \dots$$

$$B \approx 1000 \text{ mm} \quad - \text{ Ans}$$

$$1) \text{ Dia of pulley} = k_1 k_2 2P$$

$$= 2 \times 80 \times 3$$

$$D = 480 \text{ mm}$$

7) of MSQ Question Bank.

Ans). $M = 4 \text{ Tons/hr.}$

$V = 3 \text{ m/s.}$

$\rho = 2.5 \text{ tons/m}^3.$

$K_1 = 2.0$

$K_2 = 80$

i) ~~use~~ The max suitable belt inclination.
 $16-20^\circ.$

$\therefore K = 2.5 \times 10^{-4}.$

ii) $D_p = K_1 K_2 Z_p.$

$= 2 \times 80 \times 3.$

$= 480 \text{ mm}$

iii). we have $V = 3 \text{ m/s}$

$V = \frac{\pi D N}{60} \quad \therefore 3 = \frac{\pi \times 480 \times N}{60}$

$\therefore \boxed{N = 119 \text{ rpm}}$

$\therefore \text{Gear box reduction} = \frac{1440}{119} = 12.06$

8) The following data refers to a flat belt conveyor for transporting crushed rock.

Mass density ρ

$= 2 \text{ Ton/m}^3.$

Belt Speed V

$= 1.75 \text{ m/s}$

Belt width B .

$= 0.8 \text{ m.}$

Surcharge angle α

$= 25^\circ$

Determine the capacity of the belt conveyor in Tons/hr.

$$Q = c b v^2 \quad [c = \text{swirlage factor}]$$

$$= k b v^2 \quad [k = \text{flowability factor}]$$

for $\alpha = 25^\circ \quad k = 2.35 \times 10^{-4}$.

$$Q = k b v^2. \quad \text{--- (1)}$$

$$b = (0.9B - 0.05).$$

$$kg/s = \frac{kg}{m^3} \times \frac{m^3}{s}$$

$$m = \rho Q.$$

$$M = \rho Q. \quad \text{--- (2)}$$

\therefore from above

$$M = \rho k b v^2.$$

$$b = (0.9B - 0.05)$$

$$= (0.9 \times 0.8 - 0.05) m.$$

$$\boxed{b = 0.67 m.}$$

$$M = (2) \times (2.35 \times 10^{-4}) \times (1.75)^2.$$

$$M = 1.44 \times 10^{-3} \text{ Tons/sec.}$$

$$M = \rho k b^2 v$$

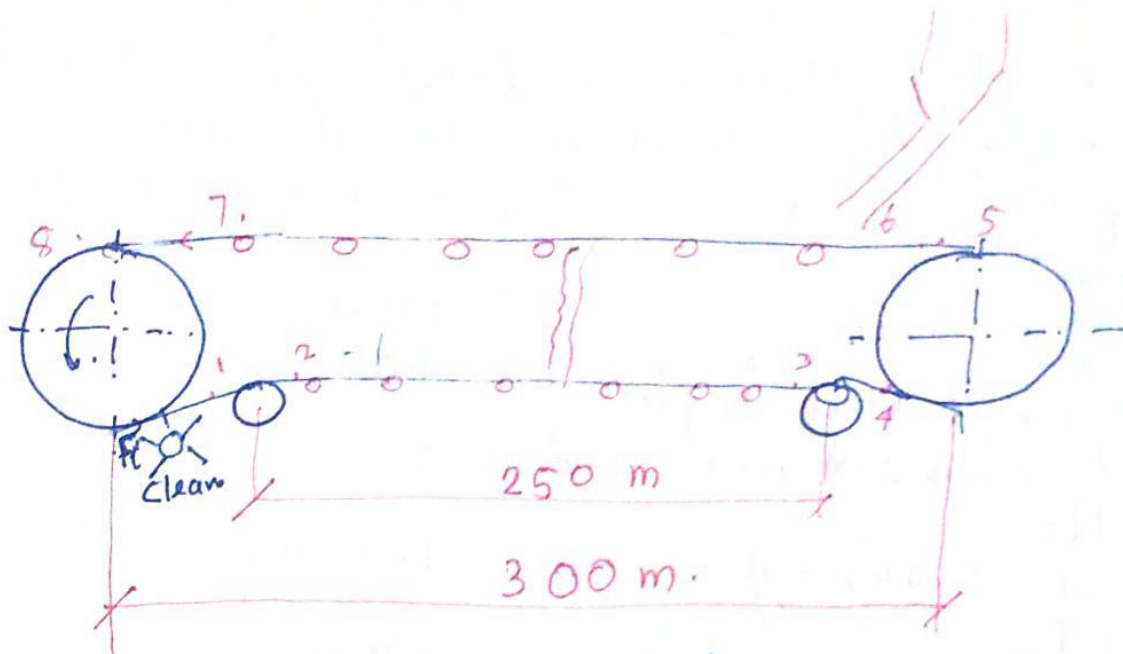
$$M = 2 \times (2.35 \times 10^{-4}) (0.67)^2 \times 1.75^2 = 6.46 \times 10^{-4} \text{ Ton/sec.}$$

$$M = 2.32 \text{ Ton/hr.}$$

- 1) The following data refers to a horizontal belt conveyor for carrying bulk material.
- Capacity of conveyor - 250 Metric Tons/hr
 - Belt speed - 1.5 m/s
 - Width of the belt - 1200 mm
 - Belt mass per unit length - 18.6 kg/m
 - Mass of each carrying run idler - 25 kg
 - Pitch of carrying run idler - 1.0 m
 - Pitch of return run idler - 2.0 m
 - Friction factor for idler - 0.02
 - Snub factor for snub pulley - 0.03
 - Snub factor for drive & tail pulley - 0.06
 - Drive & tail pulley dimensions (dia) - 500 mm
 - Frictional resistance due to belt cleaner, where $B = \text{belt width, m}$ - (100 B) N
 - Angle of lap on drive pulley - 200°
 - Coefficient of friction between belt & drive pulley - 0.4
 - Drive efficiency - 90%
 - Motor speed - 1440

Assuming that the bulk material is carried over a length of 300 meters & neglecting resistance at the loading station, determine:

- (i) the reduction ratio of gear box &
- (ii) the power required to drive the belt.



$Z_r =$ no of return run idlers.

$$Z_r \cdot \text{pitch} = L_r = \frac{L}{(Z_r + 1)}$$

$$2 = \frac{250}{Z_r + 1}$$

$$\Rightarrow \boxed{Z_r = 124}$$

similarly pitch of carrying run idlers.

$$Z_c \cdot L_c = \frac{L}{(Z_c + 1)}$$

$$1 = \frac{300}{Z_c + 1} \quad \boxed{Z_c = 299}$$

initial = F_{slack} .

At point 1

$$F_i = F_{\text{slack}} + F_{\text{clean}}$$

$$= F_{\text{slack}} + 100B$$

$$= F_{\text{slack}} + (100 \times 1.2)$$

$$\boxed{F_i = (F_s + 120)}$$

At 2.
 $F_2 = F_1 + F_{pull}$

$$= F_1 + e \cdot F_1$$

$$= (F_{slack} + 120) + 0.03(F_{slack} + 120)$$

$$= 1.03 [F_{slack} + 120]$$

$$\boxed{F_2 = 1.03 F_{slack} + 123.6}$$

At point 3

$$F_3 = F_2 + F_{RR}$$

$$F_{RR} = f_c \left(m_b + \frac{m_i z_s}{l_i} \right) g l_i$$

$$\text{Here } m_b = 18.6 \text{ kg/m}$$

$$m_i = 25$$

$$z_s = 124$$

$$l_i = 250$$

$$f_c = 0.02$$

$$F_{RR} = 0.02 \left(18.6 + \frac{25 \times 124}{250} \right) \times 9.81 \times 250$$

$$F_{RR} = 1520.55$$

$$\therefore F_3 = F_2 + F_{RR}$$

$$F_3 = 1.03 F_{slack} + 123.6 + 1520.55$$

$$\boxed{F_3 = 1.03 F_{slack} + 1644.15 \text{ N}}$$

At point 4.

$$F_4 = F_3 + e F_3$$

$$= (1 + e) F_3$$

$$F_4 = (1 + 0.03) F_3$$

$$= (1.03) [1.03 F_{slack} + 1644.15 \text{ N}]$$

$$\boxed{F_4 = 1.061 F_{slack} + 1693.5 \text{ N}}$$

At 5:

$$F_5 = F_4 + \epsilon F_4.$$

$$F_5 = (1 + \epsilon_p) F_4$$

$$F_5 = (1 + 0.06) F_4.$$

$$F_5 = (1.06) [1.061 F_{\text{slack}} + 1693.5]$$

$$\boxed{F_5 = 1.125 F_{\text{slack}} + 1795 \text{ N}}$$

At point 6

$$F_6 = F_5 + F_{1000}$$

$$F_6 = 1.125 F_{\text{slack}} + 1795 + M(v - v_1)$$

$$v_1 = 1.5, \quad \text{let } v - v_1 = 1.5 - 0.5 = 1 \text{ m/s}$$

$$F_6 = 1.125 F_{\text{slack}} + 1795 + M(1).$$

$$M = \frac{250 \times 10^3}{3600} = 69.44 \text{ kg/s.}$$

$$\cancel{F_6 = 1.125 F_{\text{slack}} + 1693.5}$$

$$\boxed{F_6 = 1.125 F_{\text{slack}} + 1864.4}$$

At 7

$$F_7 = F_6 + F_{CR}$$

$$F_{CR} = f_c \left(m_m + m_b + \frac{m_t z_c}{e} \right) l.$$

we have $M = \frac{\text{kg}}{\text{s}}$.

$$m_m = \frac{\text{kg}}{\text{m}} = \left(\frac{\text{kg}}{\text{s}} \right) \times \left(\frac{\text{s}}{\text{m}} \right) = \frac{M}{v} = \frac{69.44}{1.5}$$

$$m_m = 46.3.$$

$$F_{CR} = 0.02 \left[46.3 + 18.6 + \frac{30 \times 299}{300} \right] \times 3000 \times 98,$$

$$F_{CR} = 5580.$$

$$F_7 = 1.125 F_{\text{slack}} + 1864.4 + 5580$$

$$\boxed{F_7 = 1.125 F_{\text{slack}} + 7444.33}$$

all at points

$$g = F_7 + \epsilon_p F_7$$

$$= 1.125 F_{\text{slack}} + 0.06$$

$$= F_7 + 0.06 F_7$$

$$F_8 = (1.06) F_7$$

$$F_8 = (1.06) (1.125 F_{\text{slack}} + 7444.33)$$

$$\text{tight } F_8 = 1.192 F_{\text{slack}} + 7891$$

Also $\mu = 0.4$

$$\frac{F_{\text{tight}}}{F_{\text{slack}}} = e^{\mu \alpha}$$

$$\alpha = 200^\circ$$

$$\pi^\circ = 180^\circ$$

$$\alpha = 200$$

$$2 = \frac{200 \times \pi}{180} = 3.49800$$

$$\frac{F_{\text{tight}}}{F_{\text{slack}}} = e^{3.49 \times 0.4} = 4.04$$

$$\therefore 4.04 F_{\text{slack}} = 1.192 F_{\text{slack}} + 7891$$

$$\begin{aligned} F_{\text{slack}} &= 2771 \text{ N} \\ F_{\text{tight}} &= 11194 \text{ N} \end{aligned}$$

$$\begin{aligned} \therefore \text{Power required} &= \frac{(F_{\text{tight}} - F_{\text{slack}}) v}{1000} \\ &= \frac{(11194 - 2771) \times 1.5}{1000} \\ &= 12.63 \text{ kW} \end{aligned}$$

$$\eta = 0.9$$

$$\therefore \text{Input Power } P = \frac{12.63}{0.9} = 14 \text{ kW}$$